# SIMULATING SENSOR NETWORKS IN NS-2 [DRAFT]

Ian Downard
Naval Research Laboratory
Code 5523
4555 Overlook Ave
Washington DC, 20375-5337
downard@itd.nrl.navy.mil

June 9, 2003

#### **Abstract**

Building an optimal sensor network involves deliberately addressing each of a wide range of issues, such as physically detecting phenomena, deducing environmental information from raw sensor data, and communicating important alerts through an ad-hoc wireless network to an outside observer; all under tight energy constraints. Because of the complexity of these issues, the simulation environment provides an attractive universe for sensor network engineers to investigate the consequences of using various protocols and configurations. This was the motivation behind NRL's sensor network extensions to ns-2. In this paper, we describe how we added these extensions into the ns-2 framework, and illustrate their utility with a case study examining Mobile Ad-Hoc Network (MANET) routing within a dynamic sensor network. Finally, we will describe the limitations inherent to our simulation environment.

## 1 Introduction

Our idea of a sensor network is an autonomous, multi-hop, wireless network with nondeterministic routes over a set of possibly heterogeneous physical layers. Routing will occur throughout the network at nodes configured in ad-hoc mode. Our purpose is to evaluate how well current routing layer standards support the requirements of various layers in these sensor networks.

The primary objective of this project was to establish a foundation in ns-2 for simulating sensor networks. This paper begins with an overview of ns-2, followed by a description of our extensions to ns-2 and guidelines for using them in simulations. We conclude with a section to illustrate a sensor network simulation and a final section to list important areas for future improvement of our model.

## 2 NS-2 Overview

The ns-2 simulation environment [1] offers great flexibility to investigate the characteristics of sensor networks because it already contains flexible models for energy constrained wireless ad-hoc networks.

In the ns-2 environment, a sensor network can be built with many of the same set of protocols and characteristics as those available in the real world. The mobile networking environment in ns-2 includes support for each of the paradigms and protocols shown in Figure 1. The wireless model also includes support for node movements and energy constraints. By leveraging the existing mobile networking infrastructure, we added the capability to simulate sensor networks. The only fundamental aspect of sensor networks missing in ns-2 was the notion of a phenomenon such as chemical clouds or rolling armor that could trigger nearby sensors through a channel such as air quality or ground vibrations. Once a sensor detects the "ping" of a phenomenon in that channel, the sensor acts according to the sensor application defined by the ns-2 user. This application defines how a sensor will react once it detects its target phenomenon. For example, a sensor may periodically send a report to some data collection point as long as it continues to detect the phenomenon, or it may do something more sophisticated, such as collaborate with neighboring sensor nodes to more accurately characterize the phenomenon before alerting any outside observer of a supposed occurance. For each sensor network there is a unique sensor application to accomplish phenomena detection, surveillance, environmental monitoring, etc. With ns-2, we have provided the facility to invoke sensor applications by phenomena. With these sensor applications, we can study how the underlying network infrastructure performs under various constraints.

Figure 1: These are some of the paradigms and protocols available for wireless networking in ns-2. Some protocols like OLSR [4] and SMAC [6] have not yet been incorporated into USC's ns distributions [1], but they can be retrieved from their respective developers' sites.

## 3 Related Work

Modeling sensor networks for simulation has not received as much attention from researchers as other areas like information processing and energy conservation. In fact, we are aware of only one project whose objective included building flexible simulation tools specifically for sensor networks. Park, Savvides, Srivastava [7] developed extensions to ns-2 for this purpose, but with an emphasis on sophisticated modeling of energy consumption and emulation (i.e. interfacing with real world sensor nodes). Unfortunately, their work has not been updated to support subsequent releases of ns-2 since October, 2000.

### 4 The Extended NS-2 Architecture

Figure 2 shows where our extensions are arranged within the ns-2 framework. The major additions and modifications are explained below. Section 3.1 shows how our extensions fit into ns-2's class hierarchy.

Figure 2: This figure illustrates which files in the ns framework were modified (see left side) or added (see right side).

trace/cmu-trace.cc The CMUTrace class is used to print important parts of a packet to the simulation's trace file. Since we introduced a new packet type for phenomena, we had to describe the

corresponding packet format in this class.

- tcl/lib/ns-lib.tcl This component of the infrastructure interprets node configurations specified in the ns-2 simulation script. Our extensions introduced two new node types, the sensor node and the phenomenon node. Hence, we added some arguments in the node-config function to accommodate them.
- tcl/lib/ns-mobilenode.tcl In ns-2's virtual world, we're using its existing capacity for multichannel wireless networking as a means to emanate phenomena of various kinds. By using a dedicated channel for phenomena, we can simulate the unique physical medium that they occupy in the real world. Thus, sensor nodes will need to have two interfaces, one to the 802.11 channel and one to the PHENOM channel. We implemented this kind of "multi-homed" capability in the add-PHENOMinterface procedure of ns-mobilnode.tcl.
- common/packet.h Each packet in ns-2 is associated with a unique type that associates it with the protocol that it belongs to, such as TCP, ARP, AODV, FTP, etc. Since we created a new protocol for emanating phenomena, we defined it's corresponding packet type in the packet.h header file.
- mac/wireless-phy.cc Ns-2 contains an energy model for wireless nodes which can be used to investigate the benefits of various energy conservation techniques, such as node sleeping or utilizing optimal network densities. The model includes attributes for specifying the power requirements of transmitting packets, receiving packets, or idly standing by during times of network inactivity. Sensing phenomena is a process that may consume power at another rate, so it's important to consider this where sensor network simulations are concerned. In mac/wireless-phy.cc, we've included the capability of specifying the amount of power consumed by nodes while sensing phenomena.

We modeled the presence of phenomena in ns-2 with broadcast packets transmitted through a designated channel. The range of phenomena is the set of nodes who can receive the PHENOM broadcast packets in that channel. This pattern will follow whichever radio propagation model (free space, two ray ground, or shadowing) included with the phenomenon node's configuration. These propagation models roughly cover a circle, but other shapes could be achieved by varying the range of PHENOM broadcast packets and creatively moving a set of phenomenon nodes emanating the same type of phenomenon.

Emanating PHENOM broadcast packets is accomplished by the "PHENOM routing protocol"<sup>1</sup>, which simply broadcasts PHENOM packets with a certain configurable pulserate. When a PHENOM packet is received by a node listening on the phenomenon channel, a receive event is passed to that node's sensor application.

Every sensor network simulation must have phenomenon nodes which trigger sensor nodes, but the traffic sensor nodes generate once they detect phenomena depends on the function of the sensor network. For example, sensor networks designed for energy efficient target tracking [8] would generate more sensor-to-sensor traffic than a sensor network designed to provide an outside observer with raw sensor data. This

<sup>&</sup>lt;sup>1</sup>This functionality best fit into ns-2's existing ad-hoc wireless networking infrastructure as a routing protocol, even though it does not route at all. The MAC layer it operates above must be specified in the phenomenon node's configuration. Although real-world phenomena can interfere in a variety of ways, we ignore this aspect and use non-interfering phenomena in order to reduce the randomness of traffic patterns and simplify the analysis of routing algorithms. So, in our simulations, we configure phenomenon nodes with the basic "Mac" class, which seems to prevent channel contention.

aspect of the simulation is defined by the sensor application, which is a modular component of the simulation environment intended to be customized according to the traffic properties associated with the sensor network being simulated. The objects and functions we have just described are implemented in the following files:

phenom/phenom.cc This file implements the PHENOM routing protocol used for emanating phenomena. It includes parameters for the pulse rate and the phenomenon type (Carbon Monoxide, heavy seismic activity, light seismic activity, sound, or generic). These types are just names which can be used to identify multiple sources for phenomena in trace files. The pulse rate is the only parameter which actually controls how a PHENOM node emanates.

sensornets-NRL/sensoragent.cc The ns manual [2] describes *agents* as "endpoints where network-layer packets are constructed or consumed". Sensor nodes use a *sensor agent* attached to the PHE-NOM channel for consuming PHENOM packets, and a UDP or TCP agent attached to the wireless network channel for constructing packets sent down from the sensor application. Sensor agents act as a conduit through which PHENOM packets are received and processed by sensor applications. The sensor agent does not actually look at the contents of the PHENOM packet, it simply marks the packet as received and passes it to the sensor application. This agent is implemented in sensoragent.cc.

sensornets-NRL/sensorapp.cc The sensor application defined in this file utilizes node color and generates sensor reports to show when the corresponding sensor node detects phenomenon<sup>2</sup>. Specifically, when the node is receiving PHENOM packets, this application changes the node color to red, activates an "alarm" (public variable), and sends a sensor report of MESG\_SIZE bytes to the sink node of a UDP (or TCP) connection once per TRANSMIT\_FREQ seconds. When the node has not received a PHENOM packet in the timeout period specified by SILENT\_PHENOMENON, then the node color changes back to green. If node color is desired to illustrate energy levels instead of sensor alarm status, then that aspect of the application can be disabled with DISABLE\_COLORS.

A visualization of this sensor application is shown in Figure 3.

Figure 3: Visualization of a simulated sensor network with 25 stationary sensor nodes, 20 mobile phenom nodes simulating a gas cloud, and one stationary data collection point. The red sensor nodes detect the phenomenon, the green ones do not. The phenomenon nodes are blue, and the data collection point is black. The simulation is 20 seconds long.

## 4.1 The Extended Ns-2 Class Hierarchy

Doxygen was used to generate Figures 4, 5, and 6 which illustrate how our extensions to ns-2 fit into ns-2's class hierarchy. Dotted lines show where a class is using the methods and members of another class. Solid lines show where a class is inheriting the methods and members from another class.

<sup>&</sup>lt;sup>2</sup>The four environment variables which can be used to customize this application are SILENT\_PHENOMENON, DIS-ABLE\_COLORS, MESG\_SIZE, and TRANSMIT\_FREQ. Anytime their values are changed, the sensorapp.o file must be rebuilt (just run make on the ns-2 Makefile).

## 5 Capabilities, Guidelines, and Caveats.

This section describes the capabilities of our sensor network extensions, gives some guidelines for configuring your own simulations, and attempts to explain some areas of likely confusion. In this section, we assume the reader is already familiar with setting up mobile node simulations in ns-2. For readers who are not, you will probably have difficulty following along until you have done some basic ns-2 wireless simulations. You may find the necessary background at the following URLs:

```
http://nile.wpi.edu/NS/
http://www.isi.edu/nsnam/ns/tutorial/index.html
http://www.isi.edu/nsnam/ns/tutorial/nsscript5.html
```

The easiest way to create sensor network simulations is to use the script\_maker.pl utility in the simulations\_aids directory distributed with our extensions. This Perl script contains commonly used parameters for setting up sensor network simulations and automatically generates the often complex ns simulation script. The remainder of this section describes how to code a sensor network simulation into the ns simulation script, without using the script\_maker.pl utility.

Setting up a sensor network in ns-2 follows the same format as mobile node simulations. The best way to create your own simulation is to modify one of the examples distributed with our code [3].

Places where a sensor network simulation differs from a mobile node simulation are listed below. Setting up ns\_, god\_, tracing, topography objects and starting and stopping the simulation are all the same as in traditional mobile node simulations.

• Configure phenomenon channel and data channel.

Like mobile nodes, phenomenon nodes use 802.11 for the physical layer. So, we must configure a phenomenon channel and a data channel in order to avoid contention at the physical layer. All phenomenon nodes should be configured on the same channel, even if they're emanating different types of phenomena.

```
set chan_1 [new $val(chan)]
set chan_2 [new $val(chan)]
```

• Configure a MAC protocol for the phenomenon channel.

Choose a MAC layer to use for emanating phenomena over the phenomenon channel. Using 802.11 probably isn't appropriate, since phenomena should be emanating without regard to collisions or congestion control. We prefer using the basic "Mac" class instead.

• Configure phenomenon nodes with the PHENOM "routing" protocol:

Use node-config, just like with mobile nodes, but specify PHENOM as the routing protocol so the phenomenon is emanated according to the methods defined in phenom/phenom.cc. Also, be sure to configure in the channel and MAC layer previously specified for phenomena broadcasts.

```
$ns_ node-config \
   -adhocRouting PHENOM \
   -channel $chan_1_ \
   -llType LL \
   -macType $val(PHENOMmac) \
   -ifqType Queue/DropTail/PriQueue \
   -ifqLen 50 \
   -antType Antenna/OmniAntenna \
   -propType Propagation/TwoRayGround \
   -phyType Phy/WirelessPhy \
   -topoInstance $topo \
   -agentTrace ON \
   -routerTrace ON \
   -macTrace ON \
   -movementTrace ON
```

• Configure the Phenomenon node's pulse rate and type.

The two parameters which can be used to customize phenomena are listed below. They are both optional.

- 1. pulserate FLOAT
  - FLOAT must be a real number.
  - Describes how frequently a phenomenon node broadcasts its presence.
  - Defaults to 1 broadcast per second.
- 2. phenomenon PATTERN
  - PATTERN must be any one of the following keywords: CO, HEAVY\_GEO, LIGHT\_GEO, SOUND, TEST\_PHENOMENON corresponding to Carbon Monoxide, heavy seismic activity, light seismic activity, audible sound, and some other generic phenomenon.
  - This option is mostly useful for simulations involving multiple phenomenon nodes, so that
    it is easier to distinguish who a sensor node is detecting by looking at the NS trace file.
  - Defaults to TEST\_PHENOMENON.

```
[$node_(0) set ragent_] pulserate .1 ; #PHENOM emanates 10x/s [$node_(0) set ragent_] phenomenon CO ; #Carbon Monoxide PHENOM
```

### • Configure sensor nodes.

Sensor nodes must be configured with the -PHENOMchannel attribute and the -channel attribute. PHENOMchannel should be the same as the channel you configured the phenomenon node with. The other channel is the channel which will be used for application layer sensor reports. Also, sensor node configurations must specify a MAC protocol for the phenomena channel and a MAC protocol (such as Mac/802\_11) for the channel shared with other wireless nodes. This is done with the -PHENOMmacType and -macType attributes. PHENOMmacType should be the same as the macType used in PHENOM nodes, and macType should be the same as the macType used in other nodes participating in the MANET network (such as 802.11).

```
$ns_ node-config \
  -adhocRouting $val(rp) \
  -channel $chan_2_ \
  -macType $val(mac) \
  -PHENOMmacType $val(PHENOMmac) \
  -PHENOMchannel $chan_1_
```

If desired, a sensor node can be configured so that a specified amount of energy will be deducted from a sensor node's energy reserve each time it receives a phenomenon broadcast. To set this up, include the following parameters in the sensor node's node-config routine:

```
-energyModel EnergyModel \
-rxPower 0.175 \
-txPower 0.175 \
-sensePower 0.00000175; \
-idlePower 0.0 \
-initialEnergy 0.5
```

These parameters are described as follows:

- rxPower  $.175 \leftarrow \text{indicates } 175 mW \text{ consumed for receiving a packet of arbitrary size at time } t$
- txPower .175  $\leftarrow$  indicates 175mW consumed for transmitting a packet of arbitrary size at time t
- sensePower .00000175  $\leftarrow$  indicates  $1.75 \mu W$  consumed for detecting any amount of phenomena at time t
- initial Energy 5  $\leftarrow$  indicates a total energy reserve of 5J available to the sensor

#### *IMPORTANT CAVEAT:*

Ns-2's energy consumption model utilizes color to illustrate when a node is about to exhaust it's energy. In order to avoid confusion in the nam visualization, the node coloring which is part of the sensor application should be disabled with the DISABLE\_COLORS definition in sensorapp.cc. Remember to run make again to compile those changes into the ns executable.

In addition to DISABLE\_COLORS, some other sensor node parameters can be specified in senso-rapp.cc. These parameters are listed below:

**SILENT\_PHENOMENON** is the seconds of quiescence required for a sensor to go off it's alarming state. Example:

```
#define SILENT_PHENOMENON 0.2
```

**DISABLE\_COLORS** disables node color changes invoked by the sensor application. This is useful when it is desired to use node color to illustrate a node's energy reserves. Example:

```
#define DISABLE_COLORS FALSE
```

**MESG\_SIZE** is the size (in bytes) of the messages to send to the gateway, or data collection point, or whatever you want to call the sink node attached to this sensor node (over UDP, for example). Example:

```
#define MESG_SIZE 256
```

**TRANSMIT\_FREQ** is the frequency with which a sensor node triggered by PHENOM pkts will send a message to the the sink node attached to this sensor node. Units are in seconds, so a message of size MESG\_SIZE bytes will be transmitted to the gateway node once for every TRANSMIT\_FREQ seconds in which the sensor node has received one or more PHENOM packets.

```
#define TRANSMIT_FREQ 0.1
```

• Configure non-Sensor nodes (such as data collection points, or gateways for the sensor network).

Nodes which are not sensor nodes or phenomenon nodes, should not be configured with a PHENOM-channel, since their only interface is to the MANET network. This is done with the -PHENOMchannel "off" attribute.

```
$ns_ node-config \
  -adhocRouting $val(rp) \
  -channel $chan_2_ \
  -PHENOMchannel "off"
```

• Attach sensor agents.

Create a sensor agent for each sensor node, and attach that agent to its respective node. Also, specify that all packets coming in from the PHENOM channel should be received by the sensor agent. In the following example, \$i would represent the node number for the sensor node currently being configured.

```
set sensor_($i) [new Agent/SensorAgent]
$ns_ attach-agent $node_($i) $sensor_($i)

# specify the sensor agent as the up-target for the sensor node's link
# layer configured on the PHENOM interface, so that the sensor agent
# handles the received PHENOM packets instead of any other agent
# attached to the node.
[$node_($i) set ll_(1)] up-target $sensor_($i)
```

• Attach a UDP agent and sensor application to each node (optional).

How the sensor nodes react once they detect their target phenomenon is a behavior which should be defined as a sensor application. One such application might involve sensor nodes alerting a data collection point via UDP with information about the phenomenon. The following example illustrates how an application like that could be setup. Again, \$i represents the node number for the sensor node currently being configured.

```
set src_($i) [new Agent/UDP]
$ns_ attach-agent $node_($i) $src_($i)
```

```
$ns_ connect $src_($i) $sink

set app_($i) [new Application/SensorApp]
$app_($i) attach-agent $src_($i)
```

• Start the sensor application.

The sensor node will receive PHENOM packets<sup>3</sup> as soon as the sensor agent is attached to the node. Since the sensor agent does nothing but notify the sensor application of received phenomenon broadcasts, the sensor node does not visibly react to PHENOM packets until the sensor application has been attached and started. The following example shows how to start a sensor application:

```
$ns_ at 5.0 "$app_($i) start $sensor_($i)"
```

## 6 Case Study: MANET Routing Within a Dynamic Sensor Network

This case study begins to show the types of results one can achieve from sensor network simulations with ns-2. Suppose we'd like to characterize how well AODV scales with the size of a sensor network running the sensor application defined at the end of section 3. We will look at networks of stationary sensors with infinite energy placed in a grid with d units of distance between adjacent nodes. Our network will range from 50 sensor nodes to 2000 sensor nodes. We will limit the broadcast range of 802.11 radios and the range of the phenomenon to  $\sqrt{2d}$ , as shown in Figure 7. Since we're using the Two-ray Ground radio propagation model, nodes within this boundary always receive the broadcast and nodes outside never receive the broadcast.<sup>4</sup>

We will excite the network with a single phenomenon node which slowly travels along the perimeter of the sensor network grid. As the grid density increases, the phenomenon will encounter sensor nodes more frequently. Thus, as the grid density increases, AODV will flood more route requests through the network. As the network becomes more congested, we should observe higher latency and higher drop rates in sensor reports delivered to the stationary data collection point.

All the UDP traffic in our network consists of sensor reports, so we measured drop rates by counting the number of dropped UDP packets logged in the ns trace file.

How did we measure latency?

#### THIS SECTION IS INCOMPLETE

<sup>&</sup>lt;sup>3</sup>Phenomenon nodes start emanating immediately once the simulation starts. A delayed start can be realized by reducing the range of phenomenon broadcasts to such a small area that they are effectively inaudible to any sensors (unless they occupy the exact same coordinate in the grid). A phenomenon node can be turned off with a command like,  $ns_a t 6.0 \{[node_(si) set netif_(0)] set pt_ 0.0001\}$ . Pt\_ is the range of the broadcast, and \$i is the node id of the Phenomenon node.

<sup>&</sup>lt;sup>4</sup>In reality, this boundary is a random variable due to complex fading and interference effects.

## 7 Software References

#### 7.1 NRL Sensor Network Extensions to Ns-2

NRL's code and documentation for extending ns–2.1b9a or ns–2.26 to support sensor network simulations is available here:

```
http://pf.itd.nrl.navy.mil/projects/nrlsensorsim/
```

## 7.2 NRL OLSR Extensions to Ns-2

One of the original motivations behind building the sensor network extensions into ns-2 was to compare the behaviors of OLSR and AODV routing algorithms. NRL's OLSR extension to NS-2 is available for download via CVS [2]. To check out all the nrlolsr files (from a Linux box), type the following two commands:

```
cvs -d :pserver:anonymous@nrlolsr.pf.itd.nrl.navy.mil:/cvsroot/nrlolsr login
cvs -z3 -d :pserver:anonymous@nrlolsr.pf.itd.nrl.navy.mil:/cvsroot/nrlolsr co .
```

The instructions for including nrlolsr extensions in ns-2 are documented in nrlolsr/readme. To get the code, follow the nrlolsr-NS- link at this page:

```
http://pf.itd.nrl.navy.mil/projects/olsr/
```

## 8 Bugs

Phenomenon nodes receive broadcasts from other phenomenon nodes. This doesn't seem to effect simulation results on the IP side of the network, but it does make the simulations much longer and trace files much larger when multiple phenomenon nodes are being used in close proximity.

Please direct all bug reports to Ian Downard, <downard@itd.nrl.navy.mil>.

### 9 Future Work

Much more effort should be made to improve how phenomenon emanates. Presently, it follows the behavior of an 802.11 broadcast, configured with one of the following radio propagation models:

- 1. Free Space Model
- 2. Two Ray Ground Model
- 3. Shadowing Model

The first two models represent the communication range as an ideal circle, whose boundary is an absolute limit on signal range. The Shadowing model applies a more probabilistic means of determining whether a receiver on the boundary can receive the signal.

Using a radio propagation model to simulate anything other than electromagnetic wave propagation is probably unrealistic. So, the radio propagation model should be extended to create various phenomenon propagation models which could specifically address the characteristics of phenomena such as seismic wave propagation and gas dispersion.

## 10 Conclusion

The primary contribution of our extensions to ns-2 is the capability to invoke network traffic in manners consistent to the patterns expected for sensor networks. Our notion of sensor applications responding to a phenomenon node moving through a grid of sensor nodes is analogous to the Frisbee model [9], where the set of active sensors follows under the range of a mobile phenomenon. Coordinating these unique traffic patterns in ns-2 without our extensions requires very much effort for medium to large networks. Aside from generally increasing the flexibility of ns-2, this work facilitates our objective to evaluate how well current MANET routing protocols support the requirements of various sensor network applications.

## References

- [1] The Network Simulator ns-2, http://www.isi.edu/nsnam/ns/
- [2] The ns Manual, http://www.isi.edu/nsnam/ns/ns-documentation.html
- [3] NRL's Sensor Network Extension to ns-2, http://nrlsensorsim.pf.itd.nrl.navy.mil/
- [4] NRL's OLSR implementation for ns-2, http://pf.itd.nrl.navy.mil/projects/olsr/
- [5] Josh Broch, David A. Maltz, David B. Johnson, Yih-Chun Hu, Jorjeta Jetcheva. "A performance of Multi-Hop Wireless Ad Hoc Network Routing Protocols," in proceedings of the Fourth Annual ACM/IEEE International Conference on Mobile Computing and Networking (MOBICOM), 1998.
- [6] Wei Ye, John Heidemann, Deborah Estrin. "An Energy-Efficient MAC Protocol for Wireless Sensor Networks," in proceedings of the IEEE INFOCOM, 2002.
- [7] SensorSim: A Simulation Framework for Sensor Networks. http://nesl.ee.ucla.edu/projects/sensorsim/
- [8] H. Yang, B. Sikdar. "A Protocol for Tracking Mobile Targets using Sensor Networks," Proceedings of the First IEEE International Workshop on Sensor Network Protocols and Applications, pp. 71-81, Anchorage, AK, May 2003.
- [9] A. Cerpa, J. Elson, D. Estrin, L. Girod, M. Hamilton, and J. Zhao, "Habitat Monitoring: Application Driver for Wireless Communications Technology," Proceedings ACM SIGCOMM Workshop on Data Communications in Latin America and the Caribbean, April 2001.

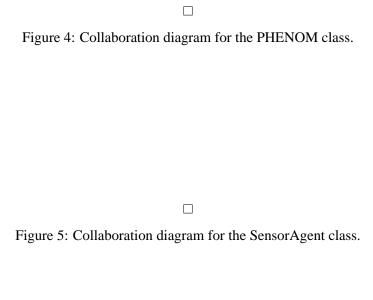


Figure 6: Collaboration diagram for the SensorApp class.

Figure 7: This figure illustrates the maximum broadcast used in our case study. If we use the Two-ray Ground radio propagation model, then the broadcast range for node 13 can never broadcast further than the ideal circle with radius  $\sqrt{2d}$ .